### Map Reduce and Streaming Calculations

Giri Iyengar

Cornell University

gi43@cornell.edu

April 16, 2018

Giri Iyengar (Cornell Tech)

Streaming Calculations

April 16, 2018 1 / 22

э

(4) (日本)

## Agenda for the week

- Map-Reduce
- Poisson resampling
- Streaming Calculations
  - Reservoir Sampling
  - Storing Items in Sets
  - Ounting in single pass
  - Frequent Items in a stream
  - Sestimating CDF/PDF in streaming mode
- Background Reading

### Overview



2 Poisson resampling

Giri Iyengar (Cornell Tech)

Streaming Calculations

April 16, 2018 3 / 22

3

<ロト < 四ト < 三ト < 三ト

#### Counting words in some text

But I must explain to you how all this mistaken idea of denouncing pleasure and praising pain was born and I will give you a complete account of the system.

- Step 0: Parse text word by word.
- Step 1: Emit one word at a time
- Step 2: Group same words together
- Step 3: Count occurrence of each word

- 4 回 ト 4 ヨ ト 4 ヨ ト

# Word Count - Emit

But	1
I	1
must	1
explain	1
to	1
you	1
how	1
all	1
this	1
mistaken	1
idea	1
of	1
denouncing	
pleasure	1

1

・ロト ・ 日 ト ・ 日 ト ・ 日 ト

# Word Count - Emit

and	1	
praising		1
pain	1	
was	1	
born	1	
and	1	
I	1	
will	1	
give	1	
you	1	
a	1	
complete		1
account		1
of	1	
the	1	
system.		1

- 2

▲□▶ ▲圖▶ ▲厘▶ ▲厘▶

# Word Count - Sort and Group

But		1		
I	1			
I	1			
a	1			
account			1	
all		1		
and		1		
and		1		
,				
born		1		
born complete		1	1	
born complete denouncing		1	1	1
born complete denouncing explain		1	1	1
born complete denouncing explain give		1	1 1	1
born complete denouncing explain give how		1 1 1	1 1	1
born complete denouncing explain give how idea		1 1 1 1	1 1	1

Giri Iyengar (Cornell Tech)

April 16, 2018 7 / 22

3

< □ > < □ > < □ > < □ > < □ >

# Word Count - Sort and Group

must	1
of	1
of	1
pain	1
pleasure	1
praising	1
system.	1
the	1
this	1
to	1
was	1
will	1
you	1
you	1

æ

< □ > < □ > < □ > < □ > < □ >

# Word Count - Aggregate

But	1		
I	2		
a	1		
account		1	
all	1		
and	2		
born	1		
complete		1	
denouncing			1
explain		1	
give	1		
how	1		
idea	1		
mistaken		1	

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

# Map Reduce



Figure: Source: highlyscalable.com blog

Giri Iyengar (Cornell Tech)

Streaming Calculations

April 16, 2018 10 / 22

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

#### MR Demo

Giri lyengar (Cornell Tech)

April 16, 2018 11 / 22

### Map Reduce Examples

• Word Count

3

<ロト < 四ト < 三ト < 三ト

- Word Count
- Unique Count

3

< □ > < □ > < □ > < □ > < □ >

- Word Count
- Unique Count
- Total Sales, Average Sales by Customer

< □ > < 同 > < 回 > < 回 > < 回 >

- Word Count
- Unique Count
- Total Sales, Average Sales by Customer
- Click-Through-Rate of Advertising Campaigns

< ∃⇒

Image: A match a ma

- Word Count
- Unique Count
- Total Sales, Average Sales by Customer
- Click-Through-Rate of Advertising Campaigns
- Little Bag of Bootstraps to Build Models

3

- ∢ ⊒ →

(A) → (A

## HDFS: Hadoop Distributed File System

HDFS Architecture



#### Figure: Source: Apache Foundation

Giri Iyengar (Cornell Tech)

Streaming Calculations

April 16, 2018 13 / 22

3

A B A A B A

# Hadoop Ecosystem



#### Figure: Source: Apache Foundation

Giri lyengar (Cornell Tech)

Streaming Calculations

April 16, 2018 14 / 22

э

< □ > < 同 > < 回 > < 回 > < 回 >

### Overview





Giri Iyengar (Cornell Tech)

Streaming Calculations

April 16, 2018 15 / 22

3

<ロト < 四ト < 三ト < 三ト

# Poisson Resampling for Efficient Bootstrapping

#### Bootstrapping Big Data

- Bootstrap is not efficient when dealing with Big Data  $\approx 63.2\%$  of data gets resampled per bootstrap
- Need several bootstrap samples depending on what you are trying to estimate (e.g. std err or percentiles)
- Little Bag of Bootstraps is one technique (saw last week)
- Poisson Resampling is another technique

< □ > < □ > < □ > < □ > < □ > < □ >

# Poisson Resampling

#### Motivation

Let's start with a tiny sample  $\{1.5, 2.5, 3.5, 4.5\}$  and do bootstrap

Sample 1	$\{1.5, 1.5, 3.5, 2.5\}$
Sample 2	$\{2.5, 1.5, 3.5, 2.5\}$
Sample 3	$\{3.5, 4.5, 4.5, 4.5\}$

We can actually describe this in terms of sample counts

Sample 1	$\{2, 1, 1, 0\}$
Sample 2	$\{1, 2, 1, 0\}$
Sample 3	$\{0, 0, 1, 3\}$

These counts follow a  $Multinomial(4,\frac{1}{4},\frac{1}{4},\frac{1}{4},\frac{1}{4},\frac{1}{4})$  distribution. Generally,  $Multinomial(n,\frac{1}{n},\ldots,\frac{1}{n})$ 

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

#### Big Data Problem

Not all data resides in the same place. Data is distributed. Also, in streaming cases, we may not even know  $\boldsymbol{n}$  in advance



Can we *approximate* bootstrapping without bringing all the data to one place?

- 4 回 ト 4 ヨ ト 4 ヨ ト

#### Approximation

What if we independently sample each data point using a  $Binomial(n, \frac{1}{n})$ ? All sampling can be done in parallel. For large n, this is *close-enough* to multinomial sampling that it doesn't matter in practice. But, we still need to know n in advance!

#### Poisson Distribution

$$\lim_{n \to \infty} Binomial(n, \frac{1}{n}) = Poisson(1)$$

 $Poisson(\lambda) = \frac{\lambda^k e^{-\lambda}}{k!}$  doesn't need to know n!

Giri Iyengar (Cornell Tech)

▲□▶ ▲□▶ ▲□▶ ▲□▶ □ ののの

#### Poisson Resampling in Action

Giri Iyengar (Cornell Tech)

Streaming Calculations

April 16, 2018 20 / 22

3

<ロト < 四ト < 三ト < 三ト

## Poisson Resampling in Map-Reduce

- Independently sample in your map task using Poisson(1)
- Emit those *k* samples
- Reducers get independent datasets, run their aggregations, and return back results
  - Aggregations could be statistics, or even entire models!

- 4 回 ト 4 ヨ ト 4 ヨ ト



Giri Iyengar (Cornell Tech)

Streaming Calculations

April 16, 2018 22 / 22